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IEEE Singapore
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Control Chapters**

**Organized and
invited by
Professor Sam Ge,
NUS**

Wireless Sensor Networks for Monitoring Machinery, Human Biofunctions, and BCW Agents

**F.L. Lewis, Assoc. Director for Research
Moncrief-O'Donnell Endowed Chair
Head, Controls, Sensors, MEMS Group**

**Automation & Robotics Research Institute (ARRI)
The University of Texas at Arlington**



Organized and
invited by
Jing Bing Zhang

Sponsored by
**SIMTech &
IEEE Singapore
Control Chapter**

Matrix Framework for Discrete Event Control



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Discrete Event Control & Decision-Making



<http://ARRI.uta.edu/acs>





香港科技大學
THE HONG KONG UNIVERSITY OF
SCIENCE AND TECHNOLOGY



Discrete Event Control

\$75K in ARO Funding for Networked Robot Workcell Control
\$80K in NSF Funding for research and USA/Mexico Network



Dr. Jose Mireles- co-PI

Objective:

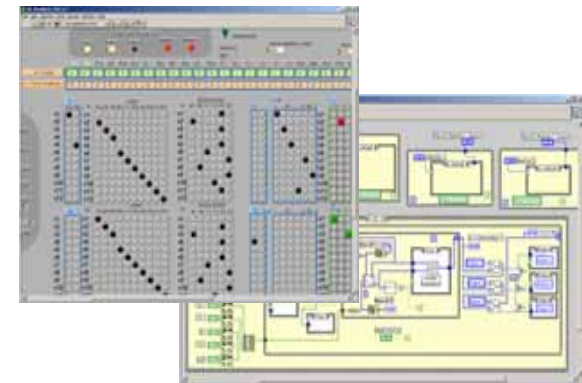
Develop new DE control algorithms for decision-making, supervision, & resource assignment WITH PROOFS

Apply to manufacturing workcell control, battlefield C&C systems, & internetworked systems

- **Patent on Discrete Event Supervisory Controller**
- **New DE Control Algorithms based on *Matrices***
- **Complete Dynamic Description for DE Systems**
- **Formal Deadlock Avoidance Techniques**
- **Implemented on Intelligent Robotic Workcell**
- **Internet- Remote Site Control and Monitoring**
- **USA/Mexico Collaboration**
- **Exploring Applications to Battlefield Systems**



Intelligent Robot Workcell



Man/Machine User Interface



USA/Mexico Internetworked Control

Matrix Formulation: Definition

Based on Manufacturing Bill of Materials

DE Model State Equation:

Compare with $x_{k+1} = Ax_k + Bu_k$

$$\bar{x} = F_v \bar{v}_c + F_r \bar{r}_c + F_u \bar{u} + F_D \bar{u}_D$$

Where multiply = AND & addition = OR

where x is the task or state logic
 F_v is the job sequencing matrix (Steward)
 F_r is the resource requirements matrix (Kusiak)
 F_u is the input matrix
 F_D is the conflict resolution matrix

Job Start Equation:

$$V_s = S_v x$$

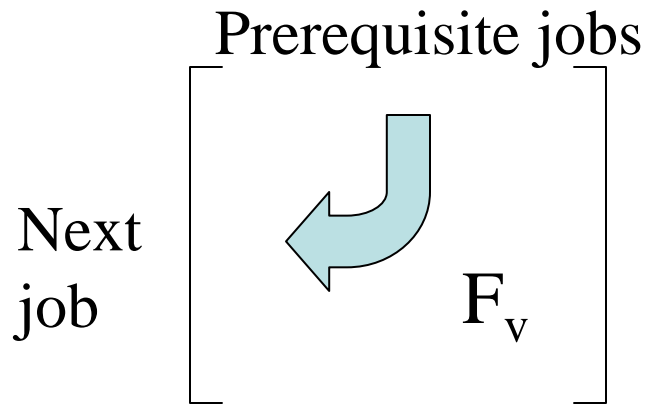
Resource Release Equation:

$$r_s = S_r x$$

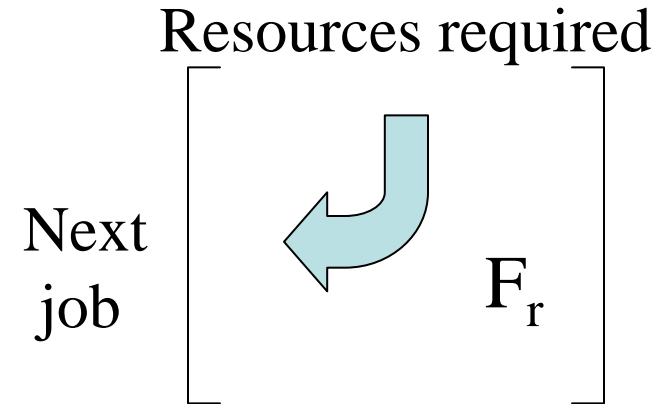
Product Output Equation:

$$y = S_y x$$

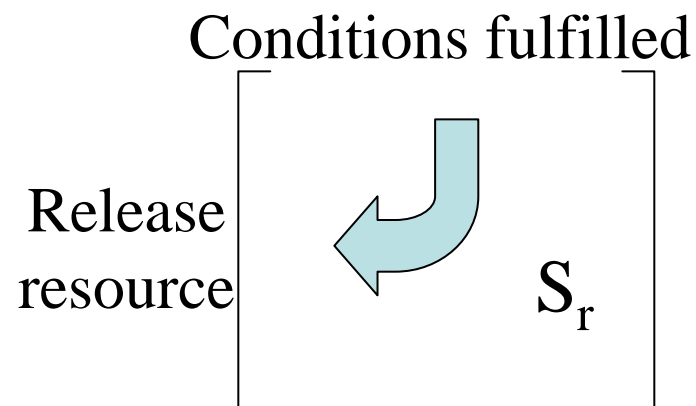
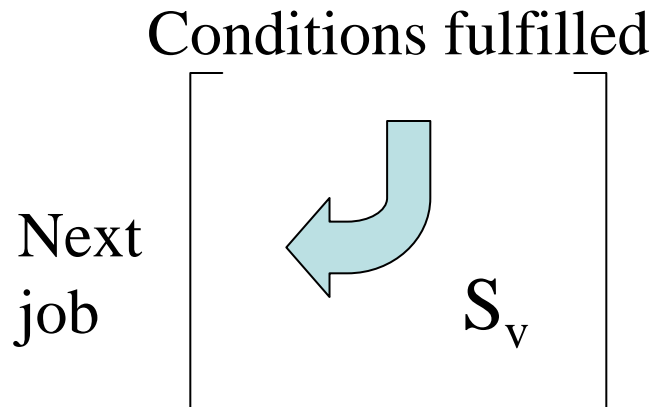
Meaning of Matrices



Steward's Task Sequencing Matrix



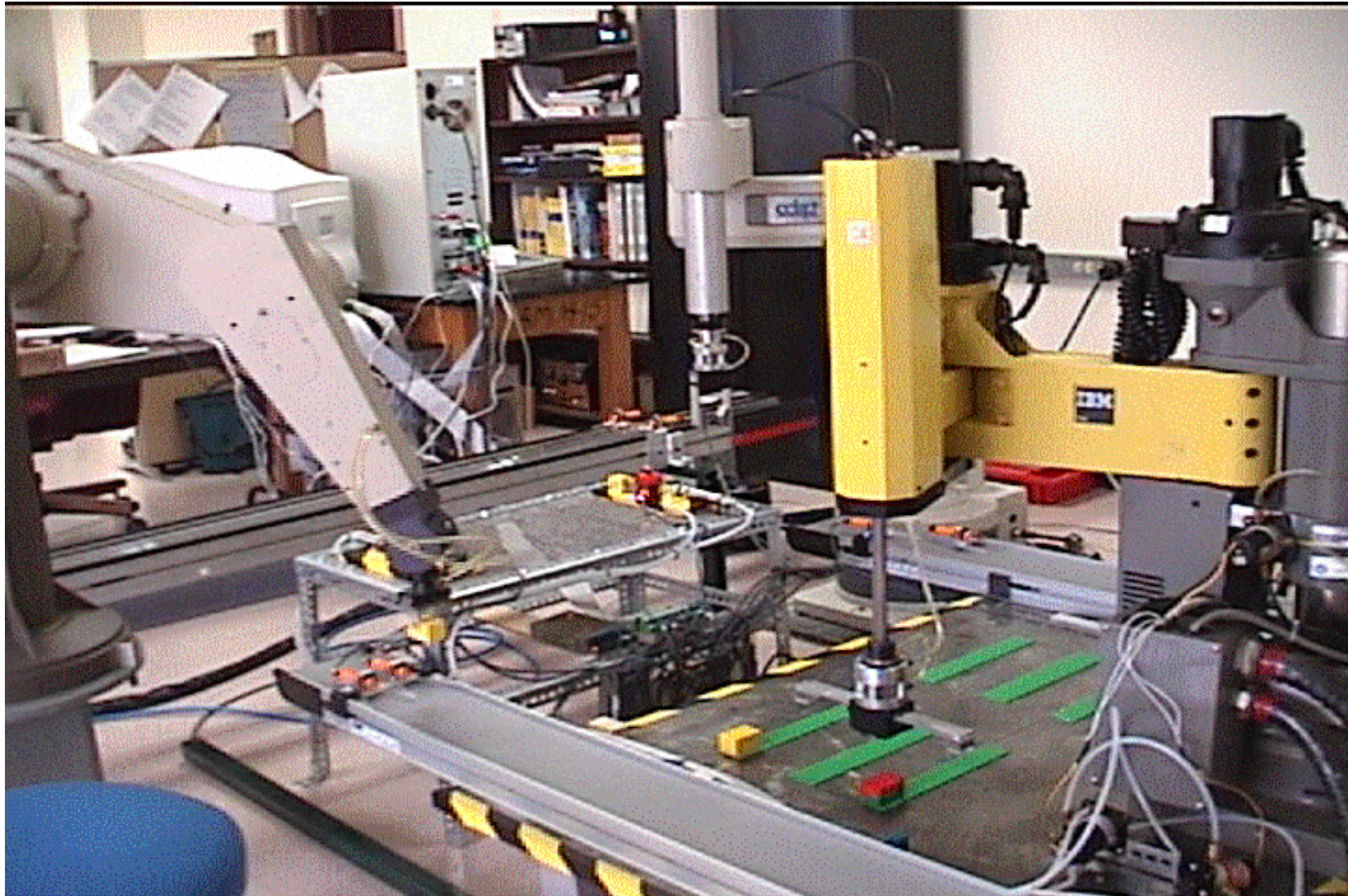
**Kusiak's Resource Requirements Matrix
Bill of Materials (BOM)**



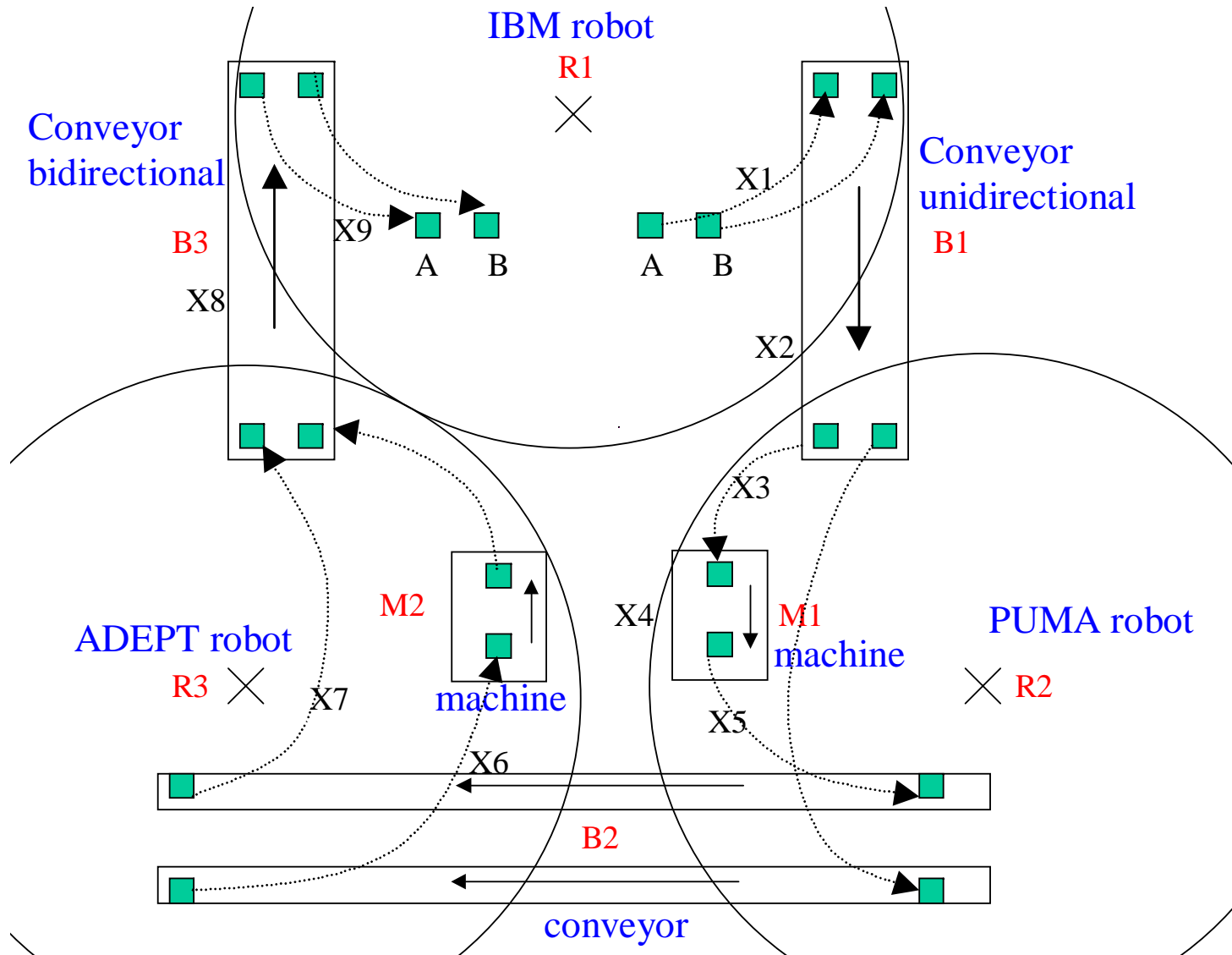
EXAMPLE

ARRI Intelligent Material Handling (IMH) Cell

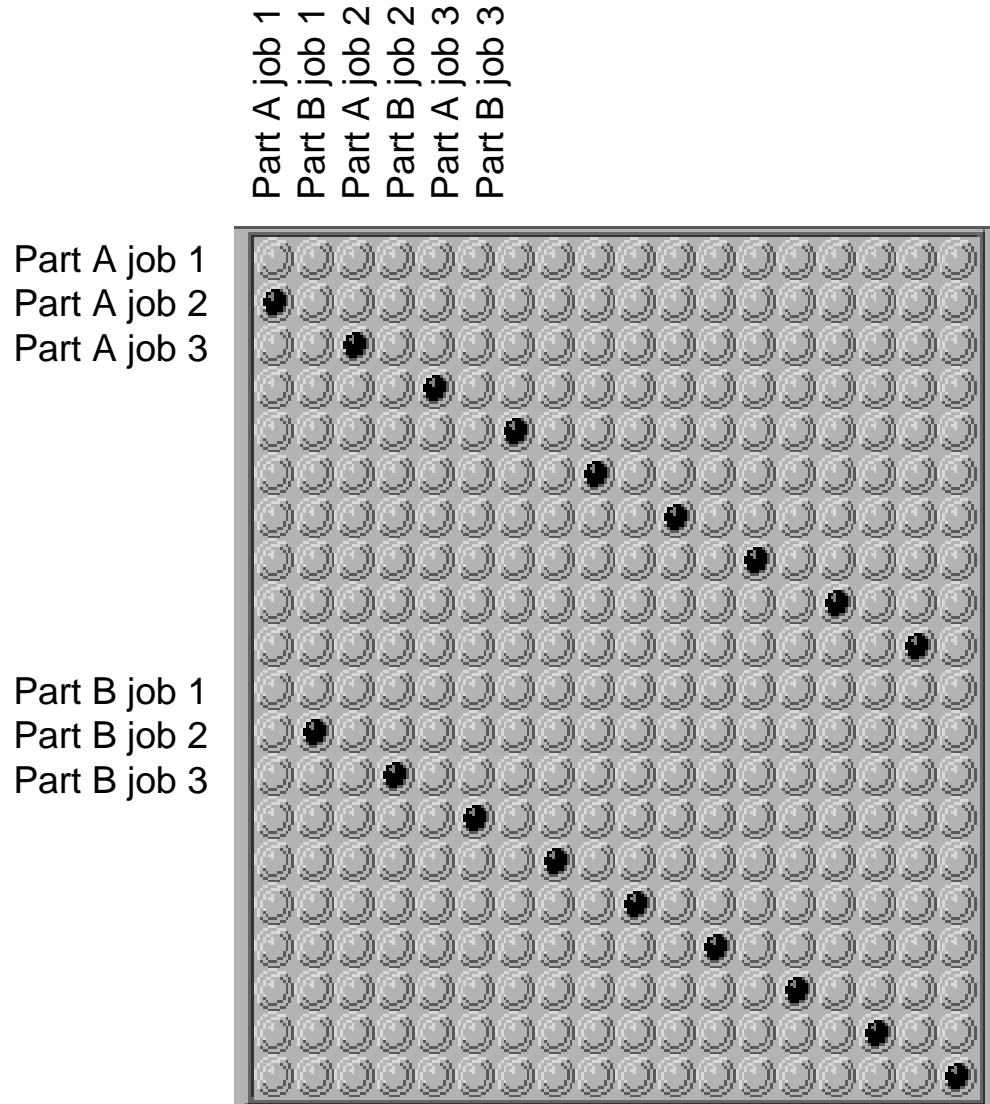
3 robots, 3 conveyors, two part paths



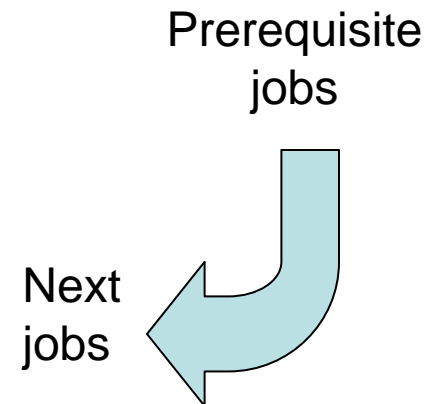
Layout of the IMH Cell



Construct Job Sequencing Matrix F_v

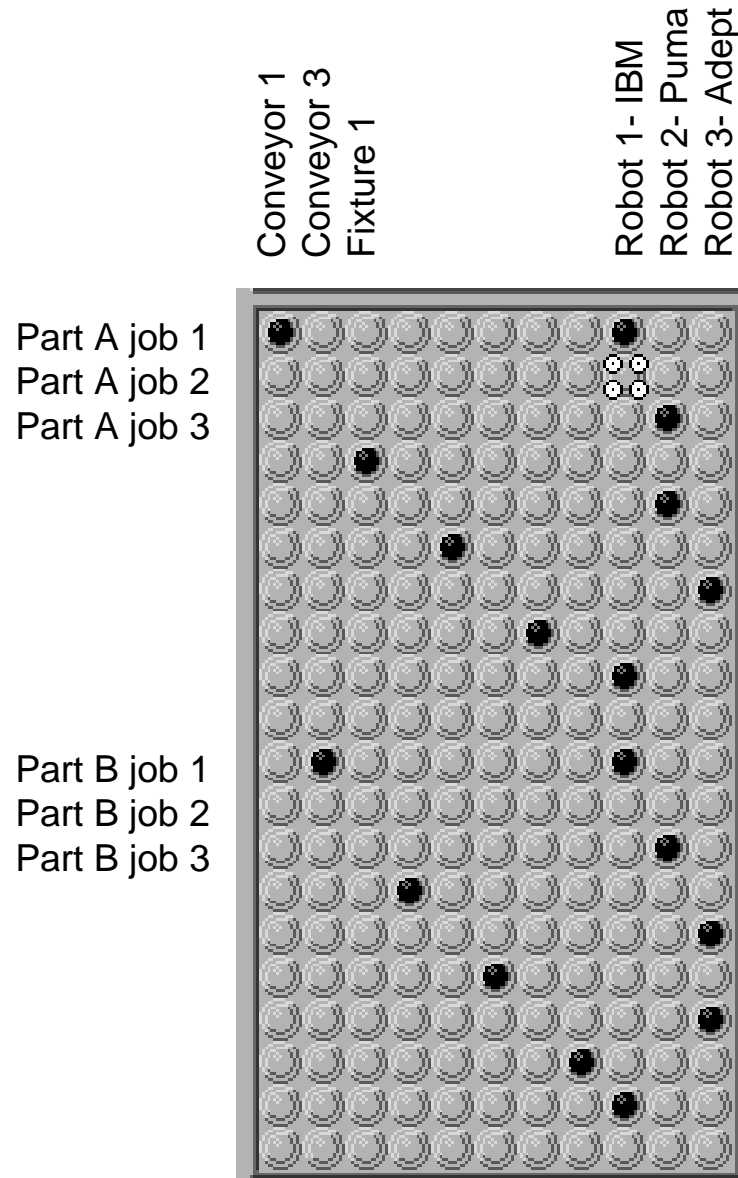


Used by Steward in
Manufacturing
Task Sequencing



Contains same information
as the Bill of Materials
(BOM)

Construct Resource Requirements Matrix F_r

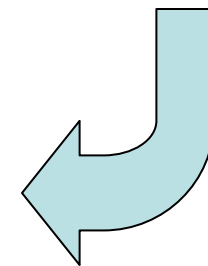


Used by Kusiak in Manufacturing Resource Assignment

Contains information about factory resources

Prerequisite resources

Next jobs



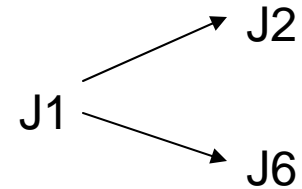
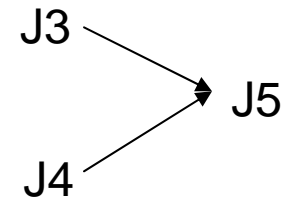
More About F_v

	J1	J3	J4
J2	1	0	0
J5	0	1	1
J6	1	0	0

Two 1's in same row = Assembly



Two 1's in same col. = Routing (Job Shop)



DECISION NEEDED!

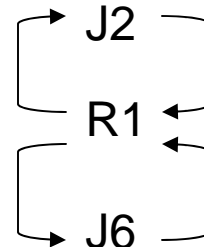
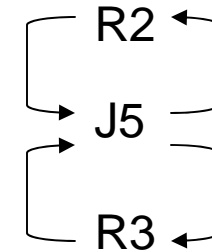
More About F_r

	R1	R2	R3
J2	1	0	0
J5	0	1	1
J6	1	0	0

Two 1's in same row = Job needs multiple res.

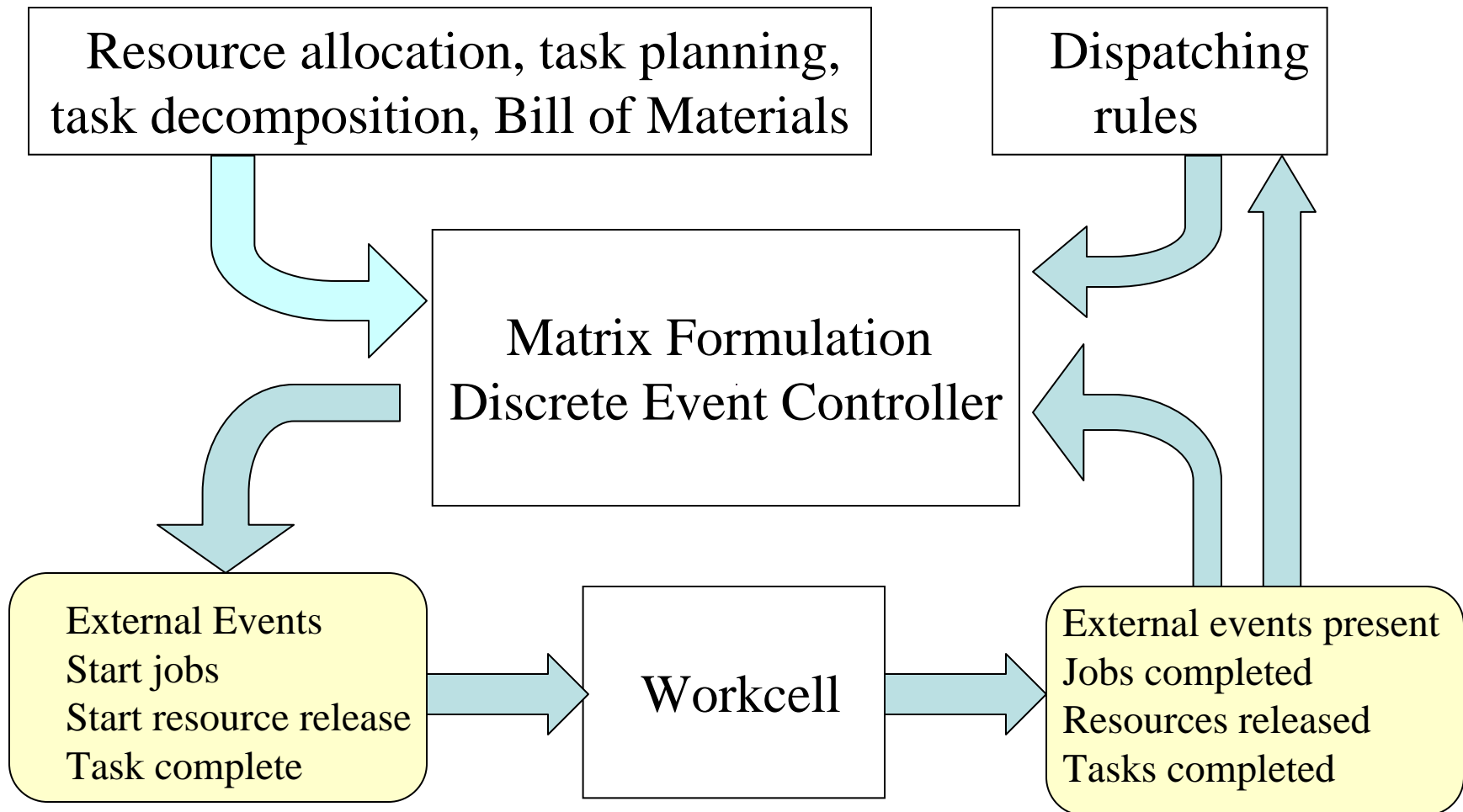


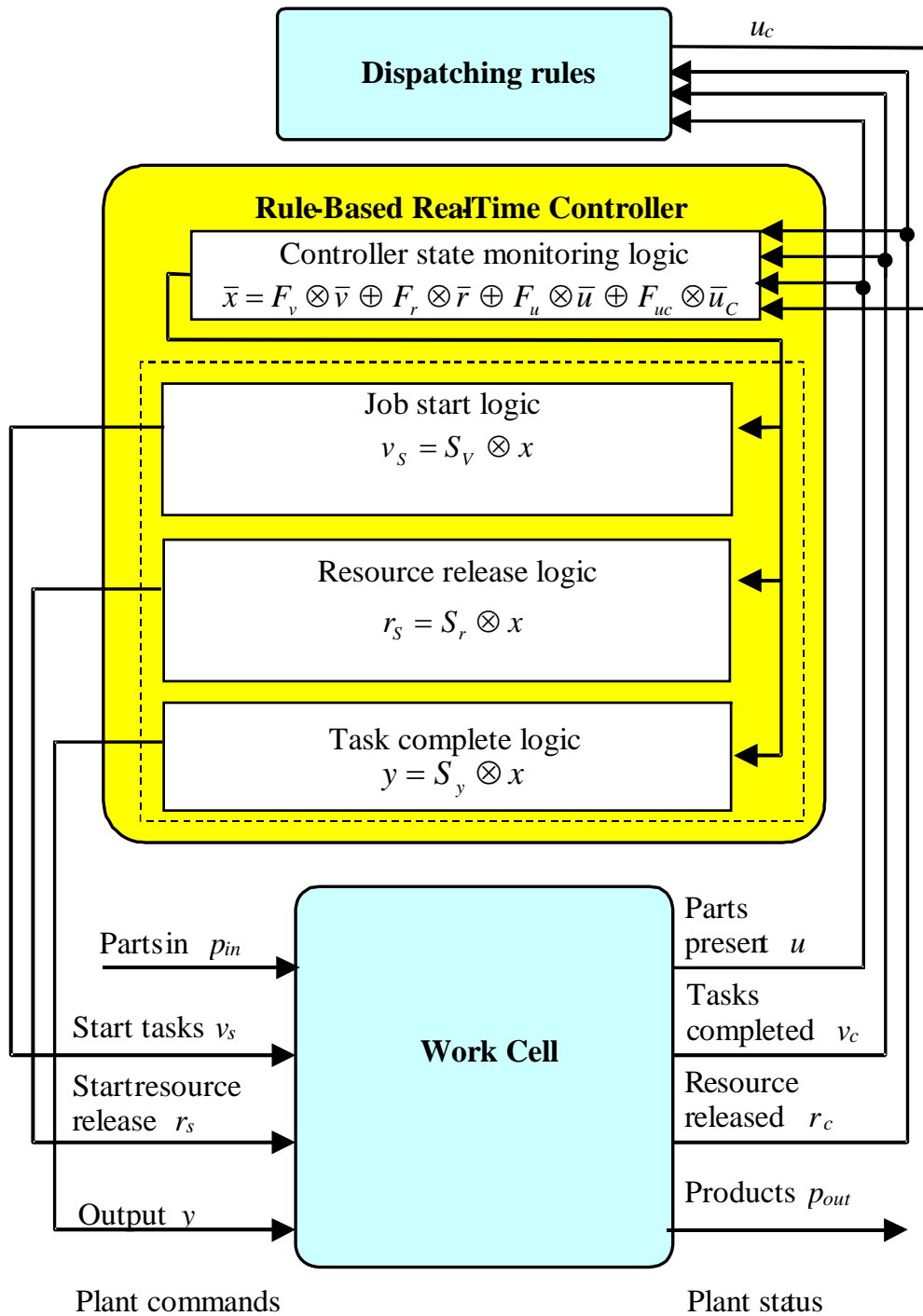
Two 1's in same col. = Shared Resource



DECISION NEEDED!

Controller based on Matrix Formulation

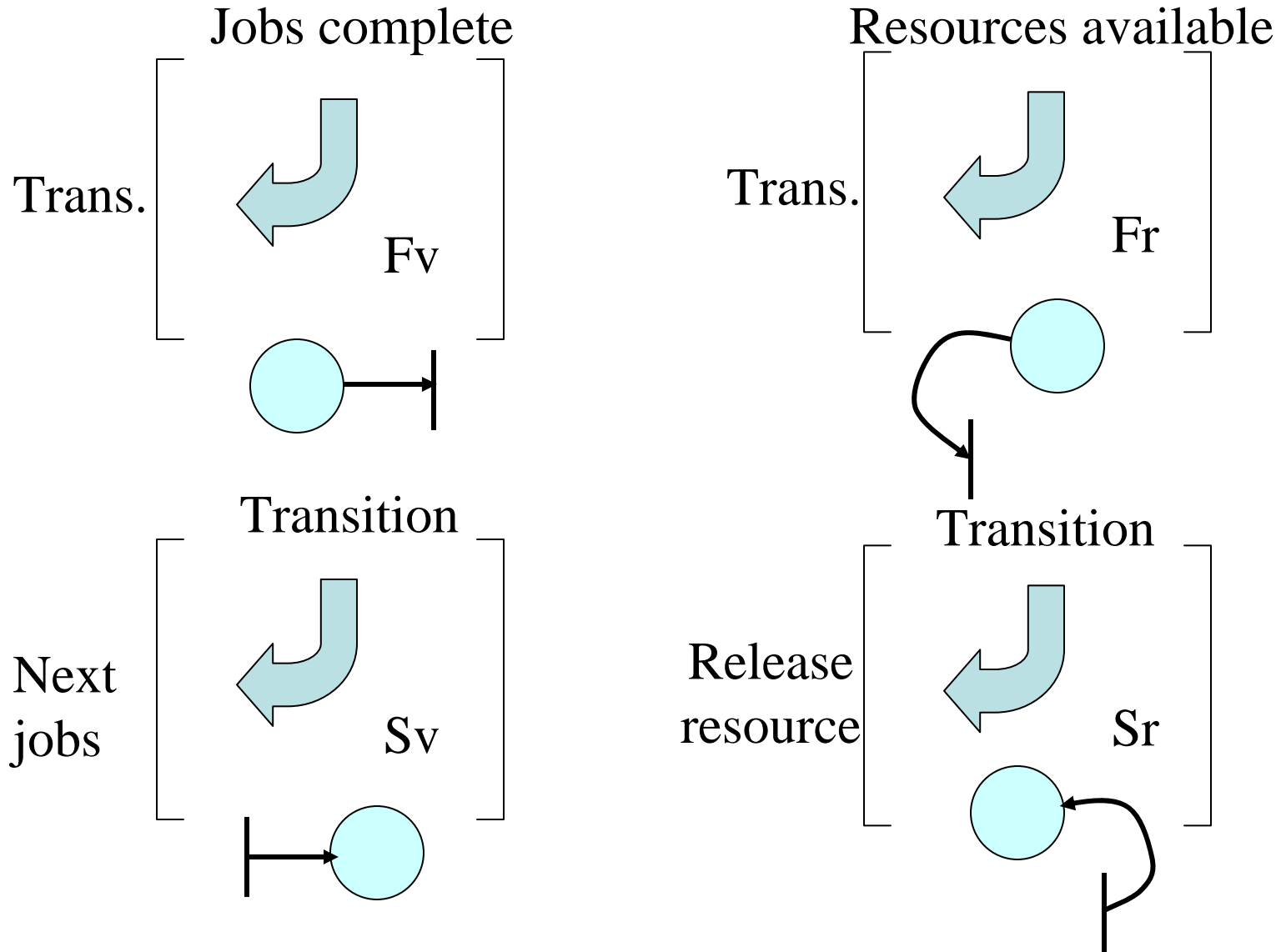




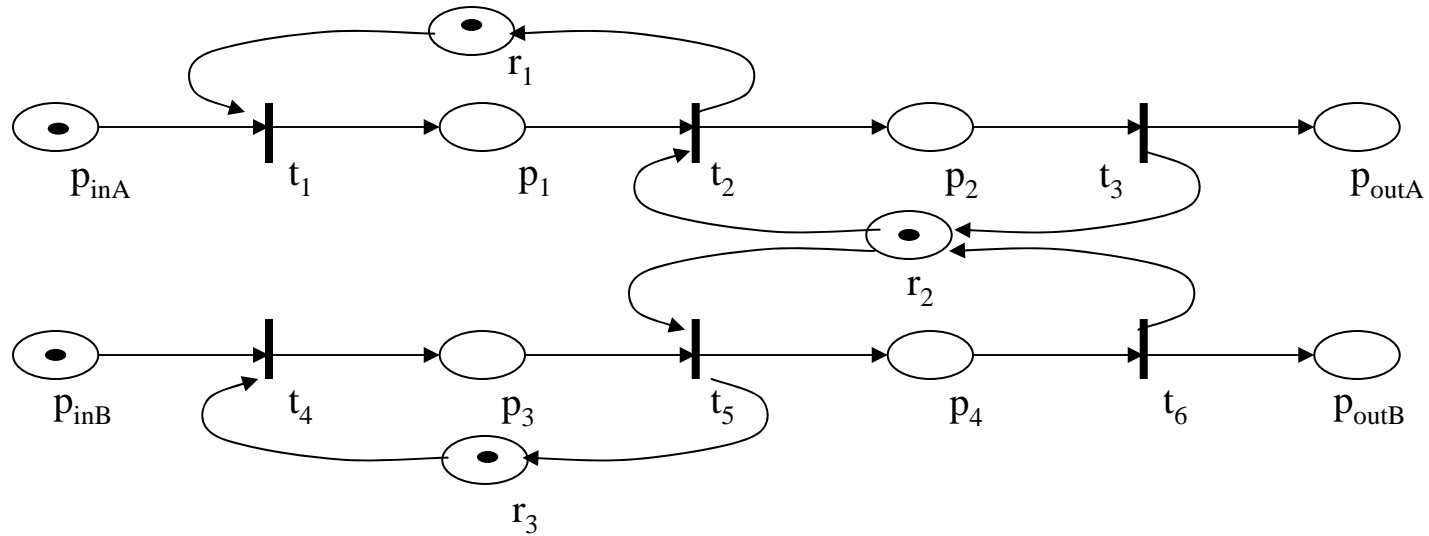
Advantages of the Matrix Formulation

- Formal rigorous framework
- Complete DE dynamical description
- Relation to known Manufacturing notions
- Formal relation to other tools- Petri Nets, MAX-Plus
- Easy to design, change, debug, and test
- Formal deadlock analysis technique
- Easy to apply any conflict resolution (dispatching) strategy
- Optimization of resources
- Easy to implement in any platform (MATLAB, LabVIEW, C, C++, visual basic, or any other)

Relation to Petri Nets



Example



$$\begin{array}{c}
 \mathbf{t_1} \\
 \mathbf{t_2} \\
 \mathbf{t_3} \\
 \mathbf{t_4} \\
 \mathbf{t_5} \\
 \mathbf{t_6}
 \end{array}
 F_v = \begin{array}{c}
 \begin{array}{cccc}
 & p_1 & p_2 & p_3 & p_4 \\
 \begin{bmatrix}
 0 & 0 & 0 & 0 \\
 1 & 0 & 0 & 0 \\
 0 & 1 & 0 & 0 \\
 0 & 0 & 0 & 0 \\
 0 & 0 & 1 & 0 \\
 0 & 0 & 0 & 1
 \end{bmatrix}
 \end{array}
 \end{array}$$

$$F_r = \begin{array}{c}
 \begin{array}{ccc}
 & r_1 & r_2 & r_3 \\
 \begin{bmatrix}
 1 & 0 & 0 \\
 0 & 1 & 0 \\
 0 & 0 & 0 \\
 0 & 0 & 1 \\
 0 & 1 & 0 \\
 0 & 0 & 0
 \end{bmatrix}
 \end{array}
 \end{array}$$

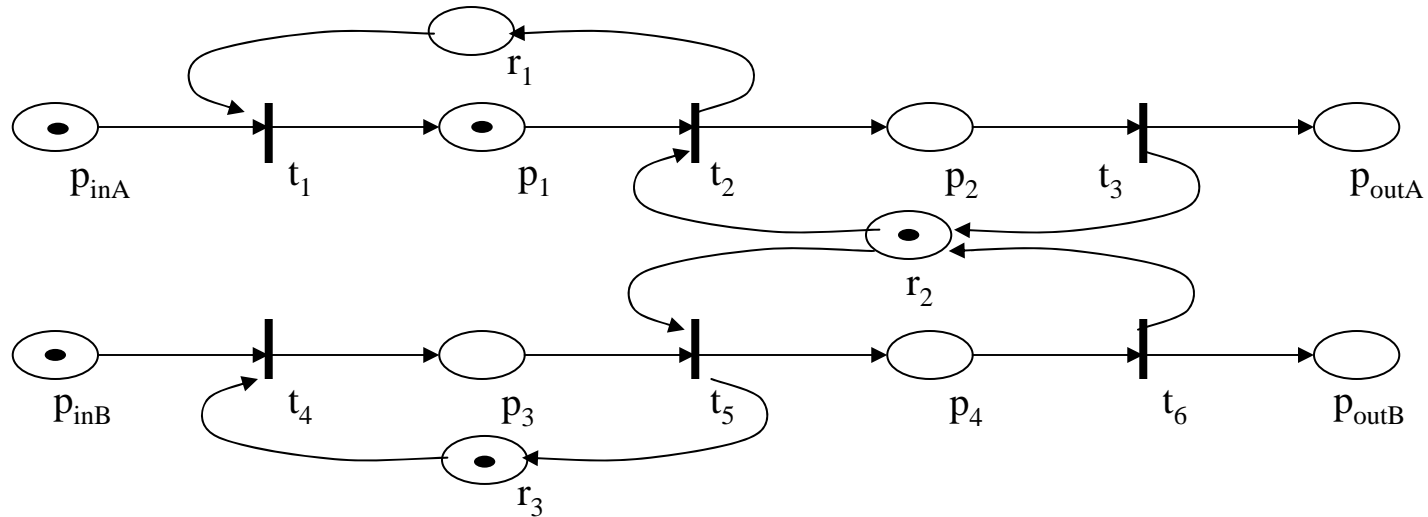
$$F_u = \begin{array}{c}
 \begin{array}{cc}
 & p_{inA} & p_{inB} \\
 \begin{bmatrix}
 1 & 0 \\
 0 & 0 \\
 0 & 0 \\
 0 & 1 \\
 0 & 0 \\
 0 & 0
 \end{bmatrix}
 \end{array}
 \end{array}$$

$$\begin{array}{c}
 \mathbf{t_1} \\
 \mathbf{t_2} \\
 \mathbf{t_3} \\
 \mathbf{t_4} \\
 \mathbf{t_5} \\
 \mathbf{t_6}
 \end{array}
 S_v^T = \begin{array}{c}
 \begin{array}{cccc}
 & p_1 & p_2 & p_3 & p_4 \\
 \begin{bmatrix}
 1 & 0 & 0 & 0 \\
 0 & 1 & 0 & 0 \\
 0 & 0 & 0 & 0 \\
 0 & 0 & 1 & 0 \\
 0 & 0 & 0 & 1 \\
 0 & 0 & 0 & 0
 \end{bmatrix}
 \end{array}
 \end{array}$$

$$S_r^T = \begin{array}{c}
 \begin{array}{ccc}
 & r_1 & r_2 & r_3 \\
 \begin{bmatrix}
 0 & 0 & 0 \\
 1 & 0 & 0 \\
 0 & 1 & 0 \\
 0 & 0 & 0 \\
 0 & 0 & 1 \\
 0 & 1 & 0
 \end{bmatrix}
 \end{array}
 \end{array}$$

$$S_y^T = \begin{array}{c}
 \begin{array}{cc}
 & p_{outA} & p_{outB} \\
 \begin{bmatrix}
 0 & 0 \\
 0 & 0 \\
 1 & 0 \\
 0 & 0 \\
 0 & 0 \\
 0 & 1
 \end{bmatrix}
 \end{array}
 \end{array}$$

OR/AND Algebra- Locating transitions firing from current marking



$$\overline{x} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \otimes \begin{bmatrix} \overline{v} \\ 0 \\ 1 \\ 1 \\ 1 \end{bmatrix} \oplus \begin{bmatrix} F_r \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} \otimes \begin{bmatrix} \overline{r} \\ 1 \\ 0 \\ 0 \end{bmatrix} \oplus \begin{bmatrix} F_u \\ 1 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 1 \\ 0 & 0 \\ 0 & 0 \end{bmatrix} \otimes \begin{bmatrix} \overline{u} \\ 0 \\ 0 \end{bmatrix}$$

$$\overline{x} = \begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \\ 1 \\ 1 \end{bmatrix} \oplus \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} \oplus \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ 1 \\ 0 \\ 1 \\ 1 \end{bmatrix}, \quad \text{SO } x = \begin{bmatrix} 0 \\ 1 \\ 0 \\ 1 \\ 0 \\ 0 \end{bmatrix} \quad \text{i.e. fire } t_2 \text{ and } t_4$$

Complete DE Dynamic Formulation

Activity Completion Matrix F :

$$F = [F_u \quad F_v \quad F_r \quad F_y]$$

Activity Start Matrix S :

$$S = [S_u^T \quad S_v^T \quad S_r^T \quad S_y^T]$$

PN Incidence Matrix:

$$M = S^T - F = [S_u^T - F_u, S_v^T - F_v, S_r^T - F_r, S_y^T - F_y]$$

PN marking transition equation:

$$m(t+1) = m(t) + M^T x = m(t) + [S^T - F]x$$

Allowable marking vector:

$$x_k = \bar{F} \oplus \bar{\bar{m}}_k = \overline{[F_u \quad F_v \quad F_r \quad F_y]} \oplus \overline{\overline{[PI \quad v \quad r \quad PO]}}_k$$

Petri Net Marking Transition Equation-- need to add Job Duration Times

$$m(t) = m_a(t) + m_p(t)$$

PN Marking Vector

Split transition equation in two steps

$$m_p(t+1) = m_p(t) + S^T x(t)$$

Add tokens

$$m_a(t+1) = m_a(t) - F x(t)$$

Subtract tokens when job complete

$$T = [O, vtimes^T, rtimes^T, O]^T$$

Add Time Duration Vector

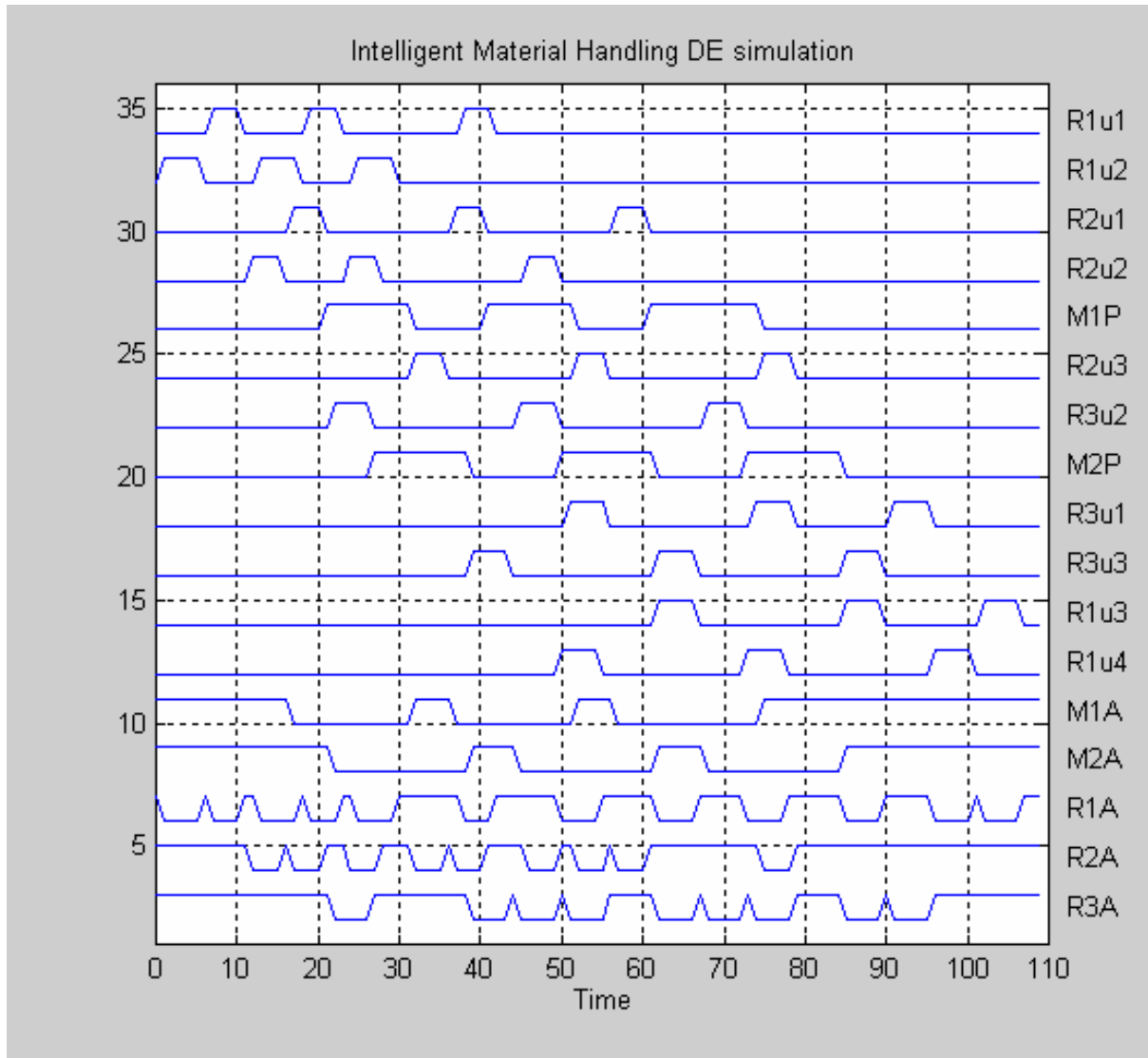
$$T_{pend}(t+1) = diag\{m_p(t)\}[T_{pend}(t) - t_{sample}] + diag\{S^T x(t)\}T$$

$$m_p(t) = m_p(t) - m_{finish}(t)$$

$$m_a(t) = m_a(t) + m_{finish}(t)$$

Corresponds to Timed Places

Allows Direct Simulations- e.g. MATLAB



c.f. DE version
of ODE23

Jobs completed
by Robot 1

Robot 1
busy or idle

Relation to Max-Plus Algebra

$$\bar{x} = F_v \bar{v}_c + F_r \bar{r}_c + F_u \bar{u} + F_D \bar{u}_D \quad \text{State equation}$$

$$V_s = S_v x$$

$$r_s = S_r x$$

$$y = S_y x$$

Output equations

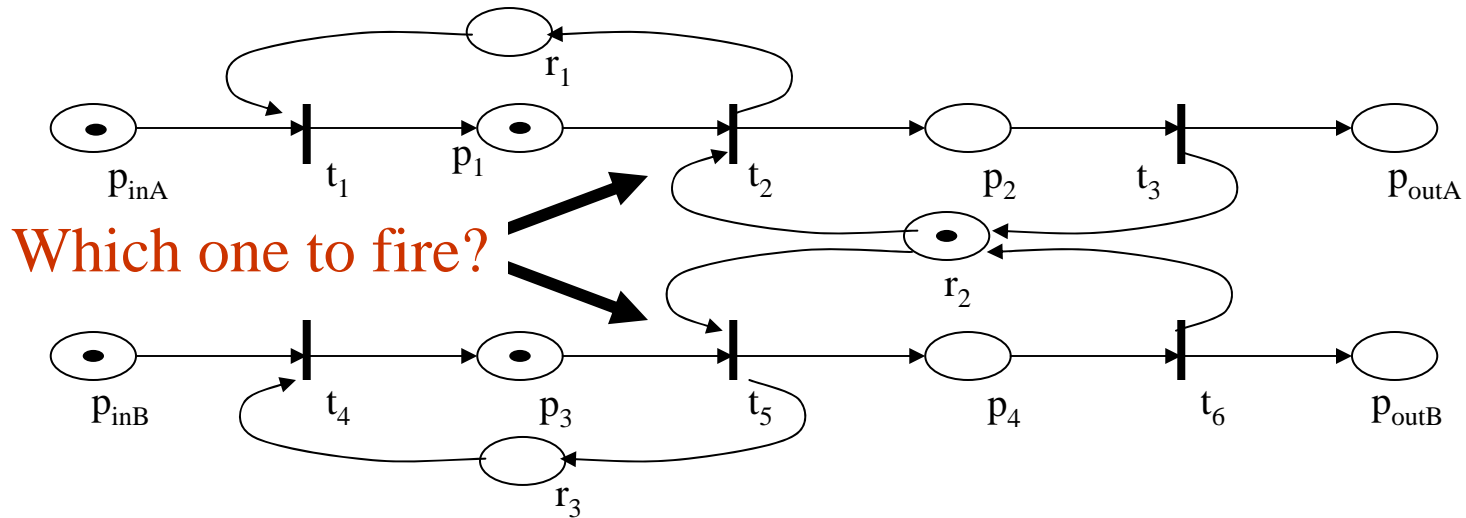
OPERATIONS IN OR-AND ALGEBRA

Define timing matrices. Then max plus is

$$x' = S_v T_v F_v x + S_r T_r F_r r \quad \text{OPS. IN MAX-PLUS ALGEBRA}$$

Can also include nonlinear terms- correspond to decisions

Conflict Resolution for Shared Resources



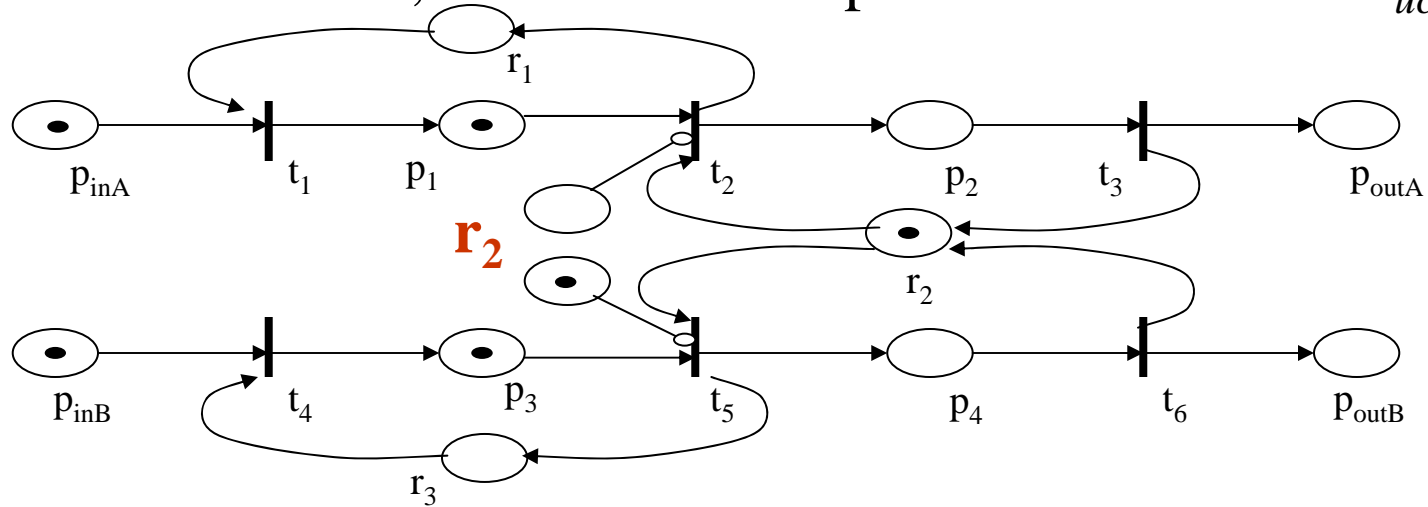
$$\overline{x} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \otimes \begin{bmatrix} \overline{v} \\ 0 \\ 1 \\ 0 \\ 1 \end{bmatrix} \oplus \begin{bmatrix} F_r \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} \otimes \begin{bmatrix} \overline{r} \\ 1 \\ 0 \\ 1 \end{bmatrix} \oplus \begin{bmatrix} F_u \\ 1 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 1 \\ 0 & 0 \\ 0 & 0 \end{bmatrix} \otimes \begin{bmatrix} \overline{u} \\ 0 \\ 0 \end{bmatrix}$$

Shared Resource- Two entries in same column

$$\begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \\ 0 \\ 1 \end{bmatrix} \oplus \begin{bmatrix} 1 \\ 0 \\ 0 \\ 1 \\ 0 \\ 0 \end{bmatrix} \oplus \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ 1 \\ 1 \\ 0 \\ 1 \end{bmatrix}, \text{ so } x = \begin{bmatrix} 0 \\ 1 \\ 0 \\ 0 \\ 1 \\ 0 \end{bmatrix}$$

But gives negative marking!
Cannot fire both.

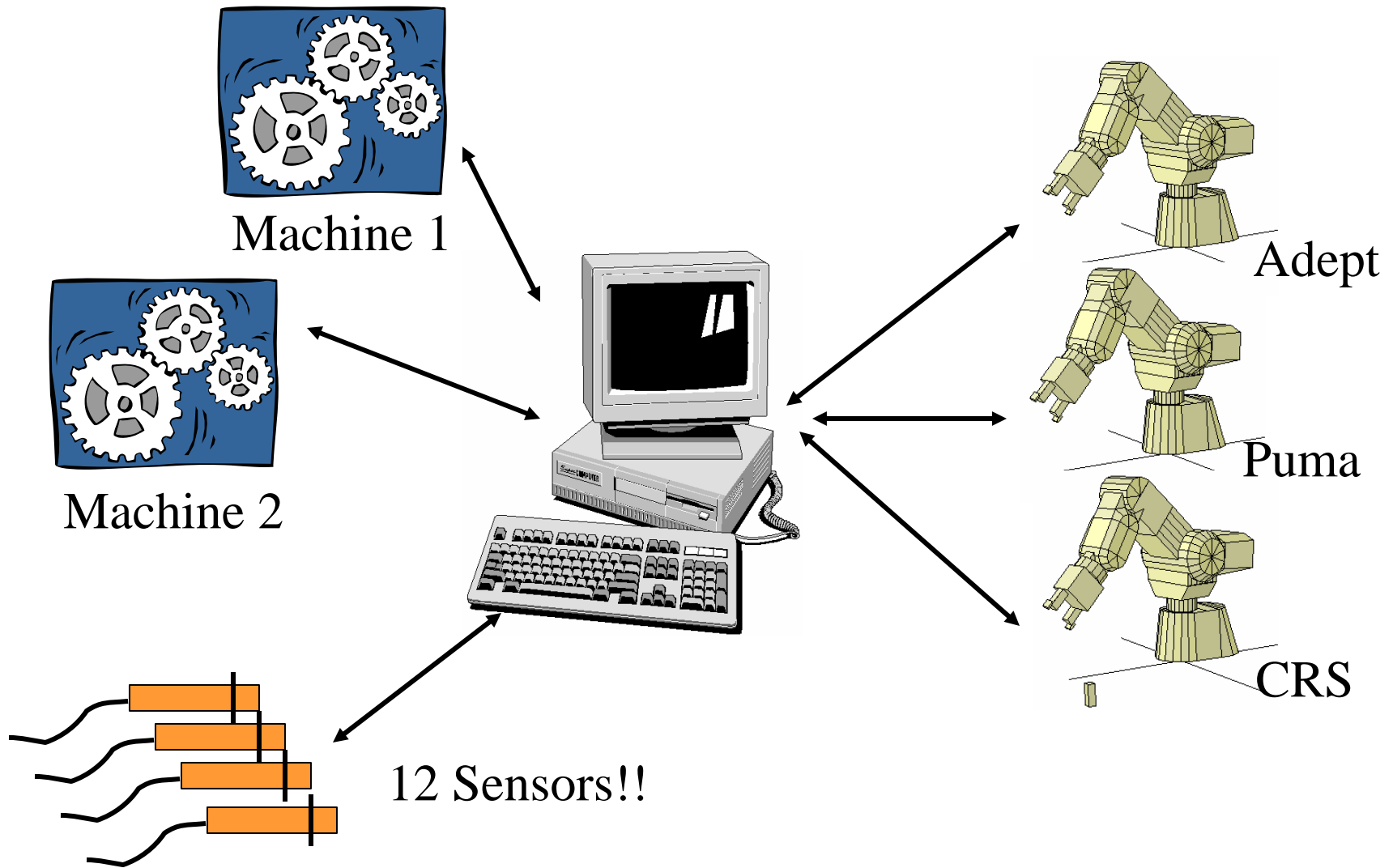
Conflict resolution, add extra CR input and new matrix F_{uc} :



$$\overline{x} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} F_v \overline{v} \oplus \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} F_r \overline{r} \oplus \begin{bmatrix} 1 & 0 \\ 0 & 0 \\ 0 & 1 \end{bmatrix} F_u \overline{u} \oplus \begin{bmatrix} 0 & 0 \\ 1 & 0 \\ 0 & 0 \\ 0 & 1 \\ 0 & 0 \end{bmatrix} F_{uc} \overline{r_2}$$

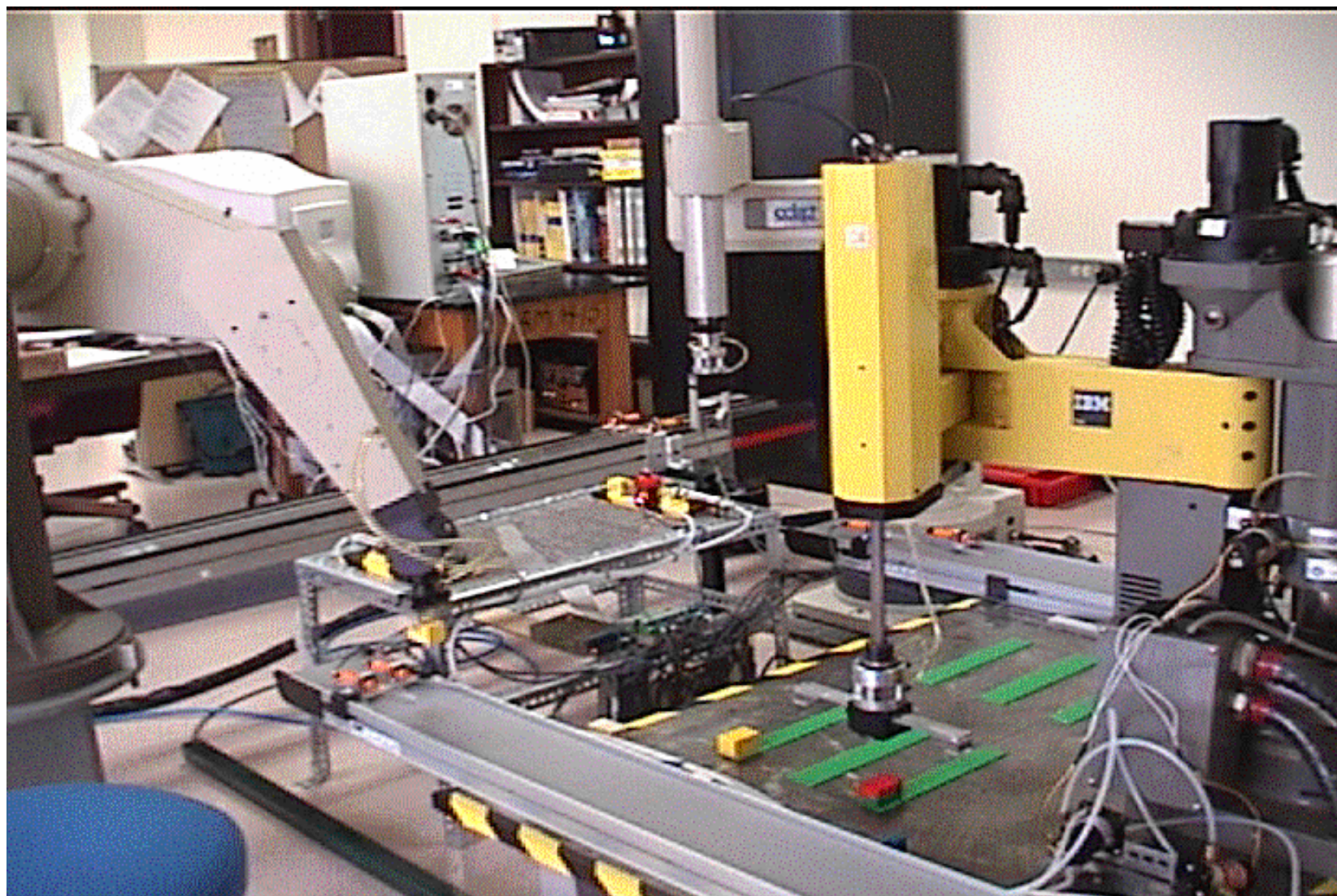
$$\begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \\ 0 \\ 1 \end{bmatrix} \oplus \begin{bmatrix} 1 \\ 0 \\ 0 \\ 1 \\ 0 \\ 0 \end{bmatrix} \oplus \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} \oplus \begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \\ 0 \\ 1 \end{bmatrix}, \text{ so } x = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \\ 0 \end{bmatrix} \rightarrow \text{Now only } t_5 \text{ fires}$$

Application- Intelligent Material Handling

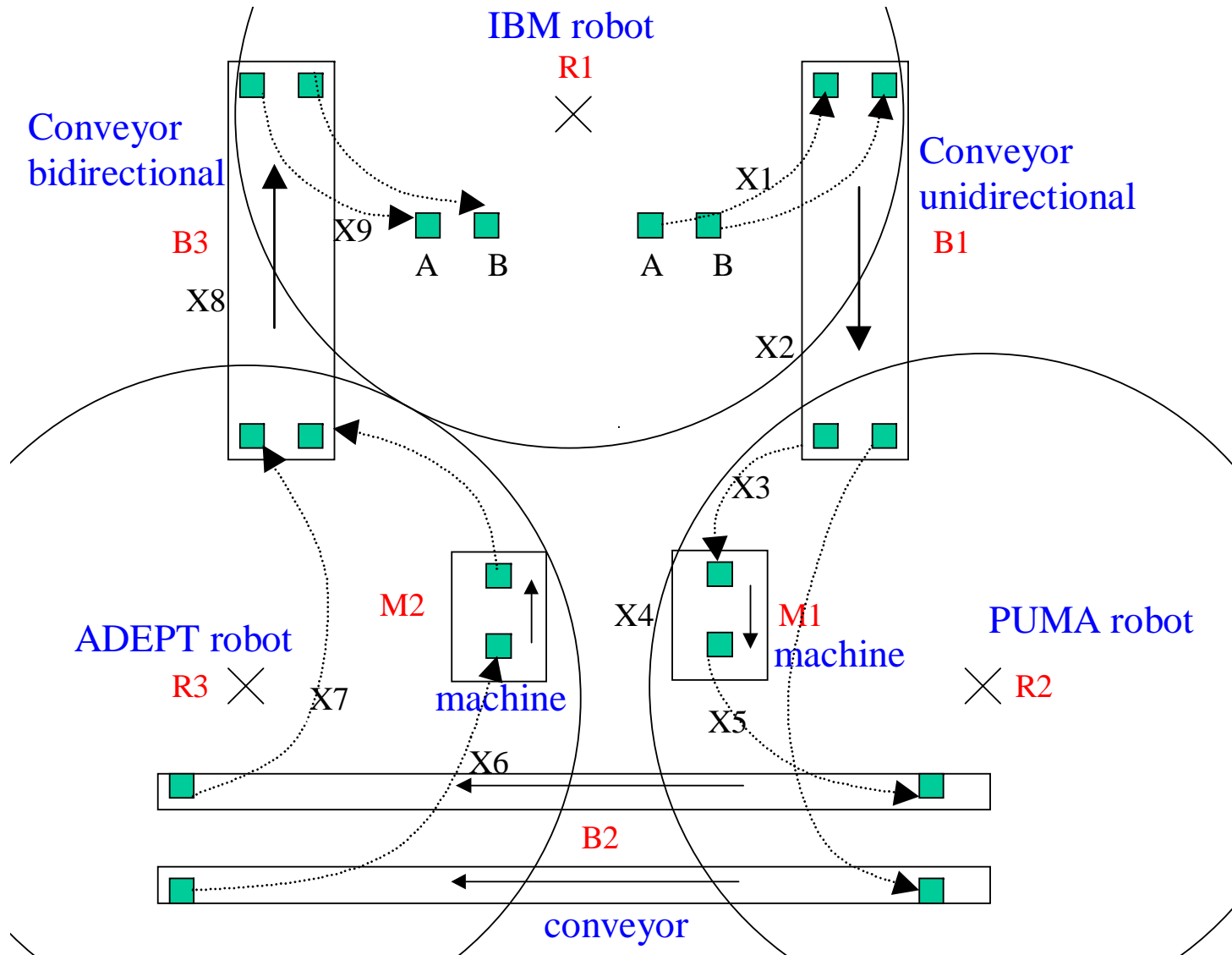


ARRI Intelligent Material Handling (IMH) Cell

3 robots, 3 conveyors, two part paths

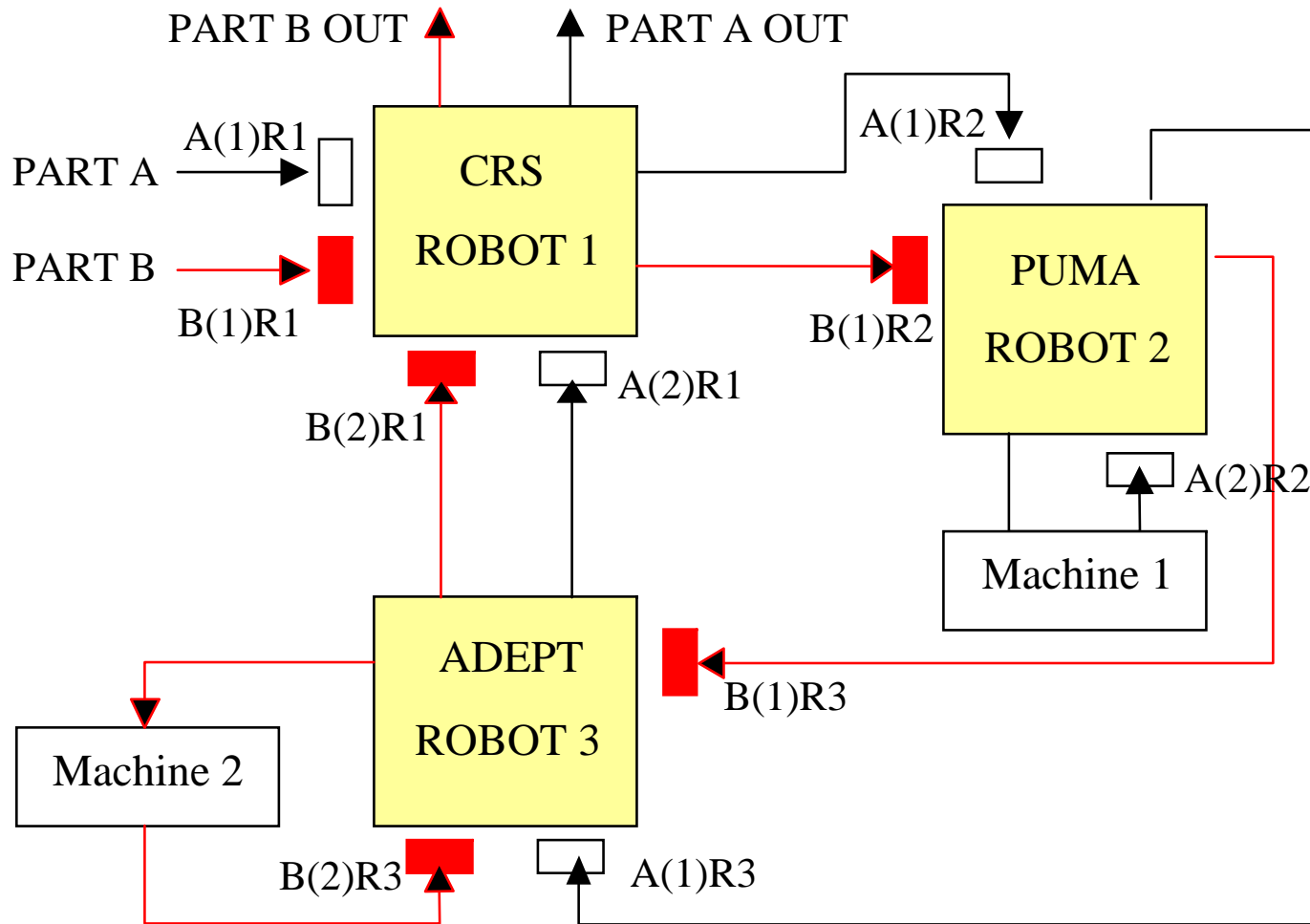


Layout of the IMH Cell

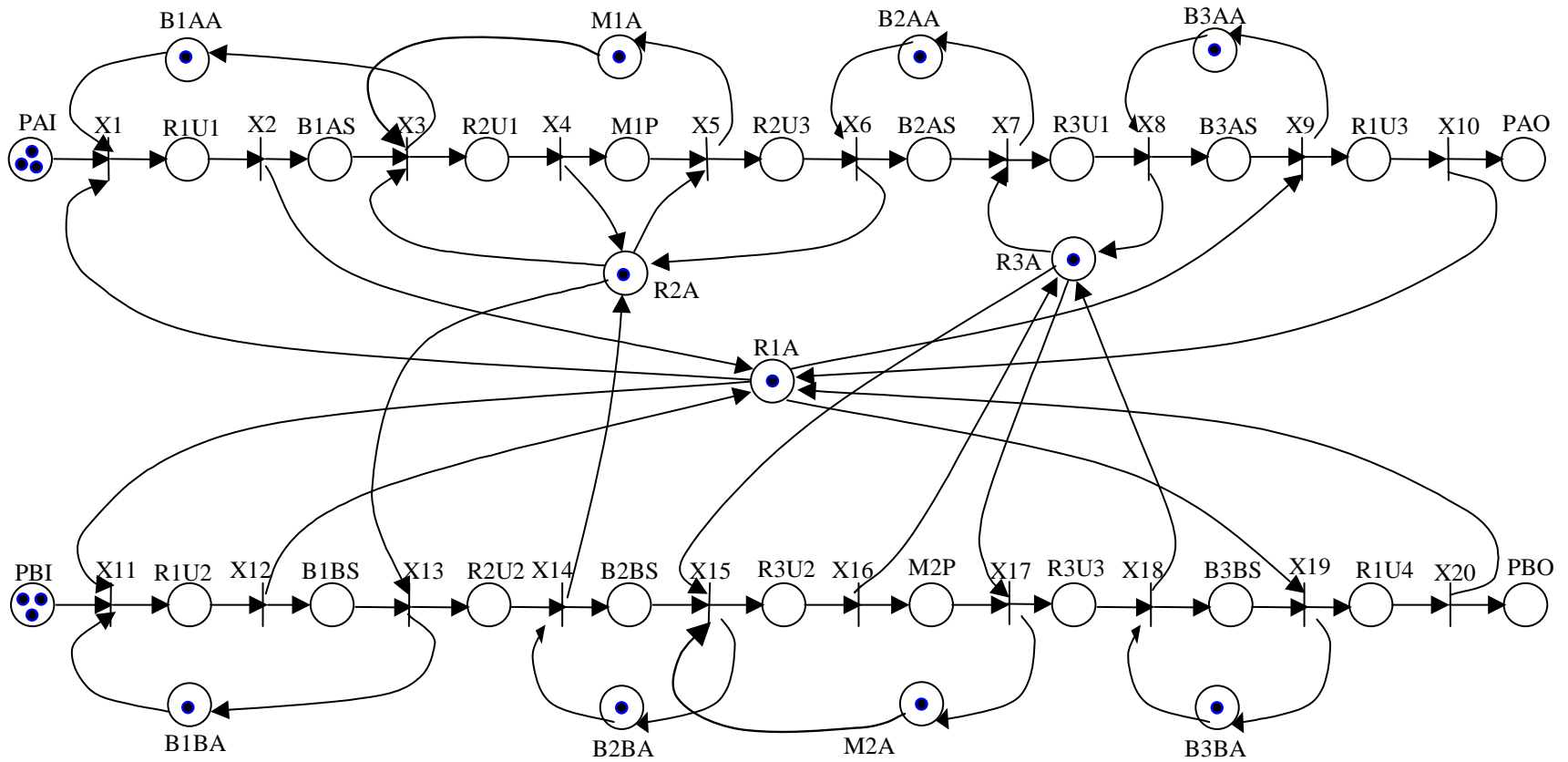


Multipart Reentrant Flow Line

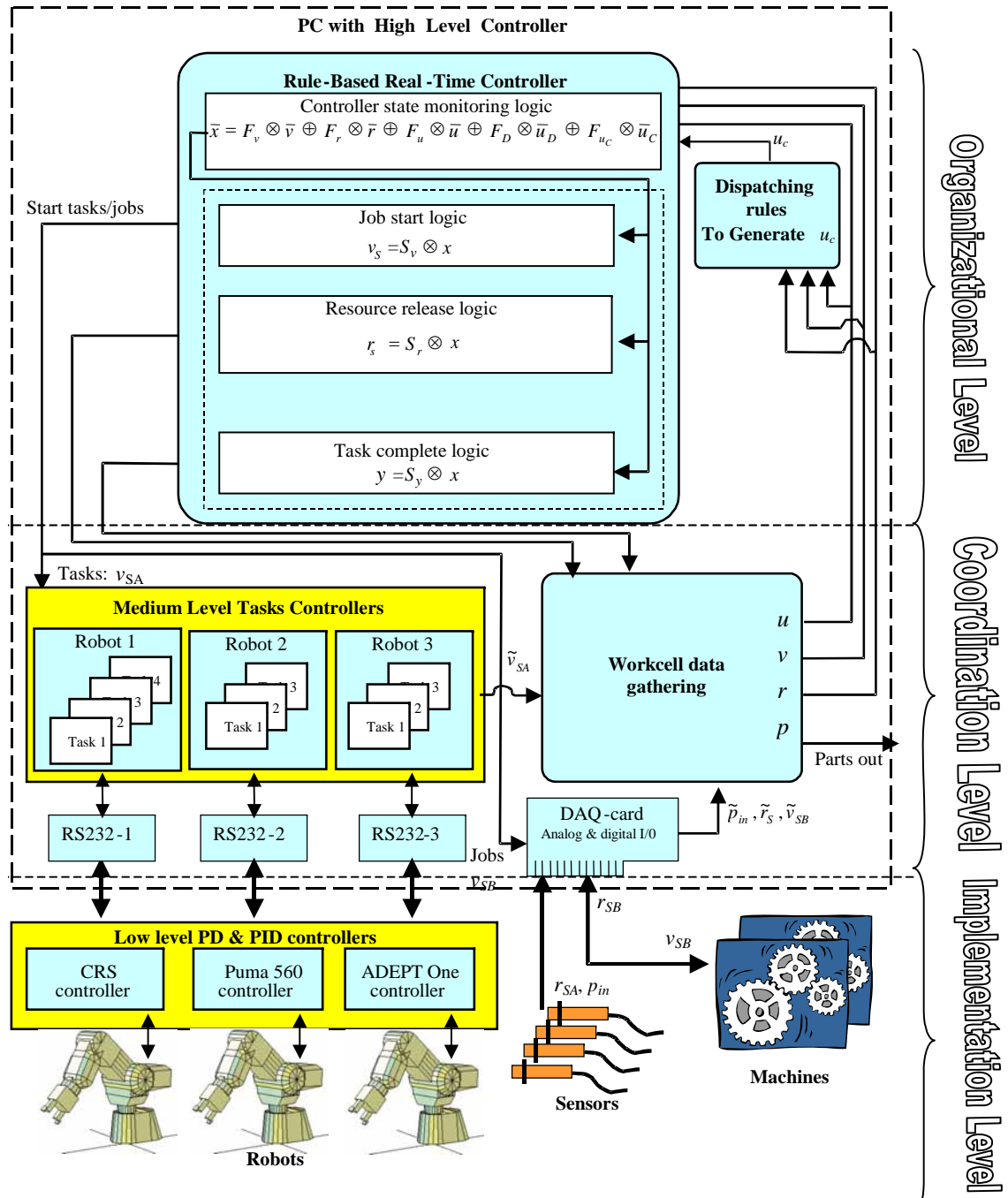
c.f. Kumar



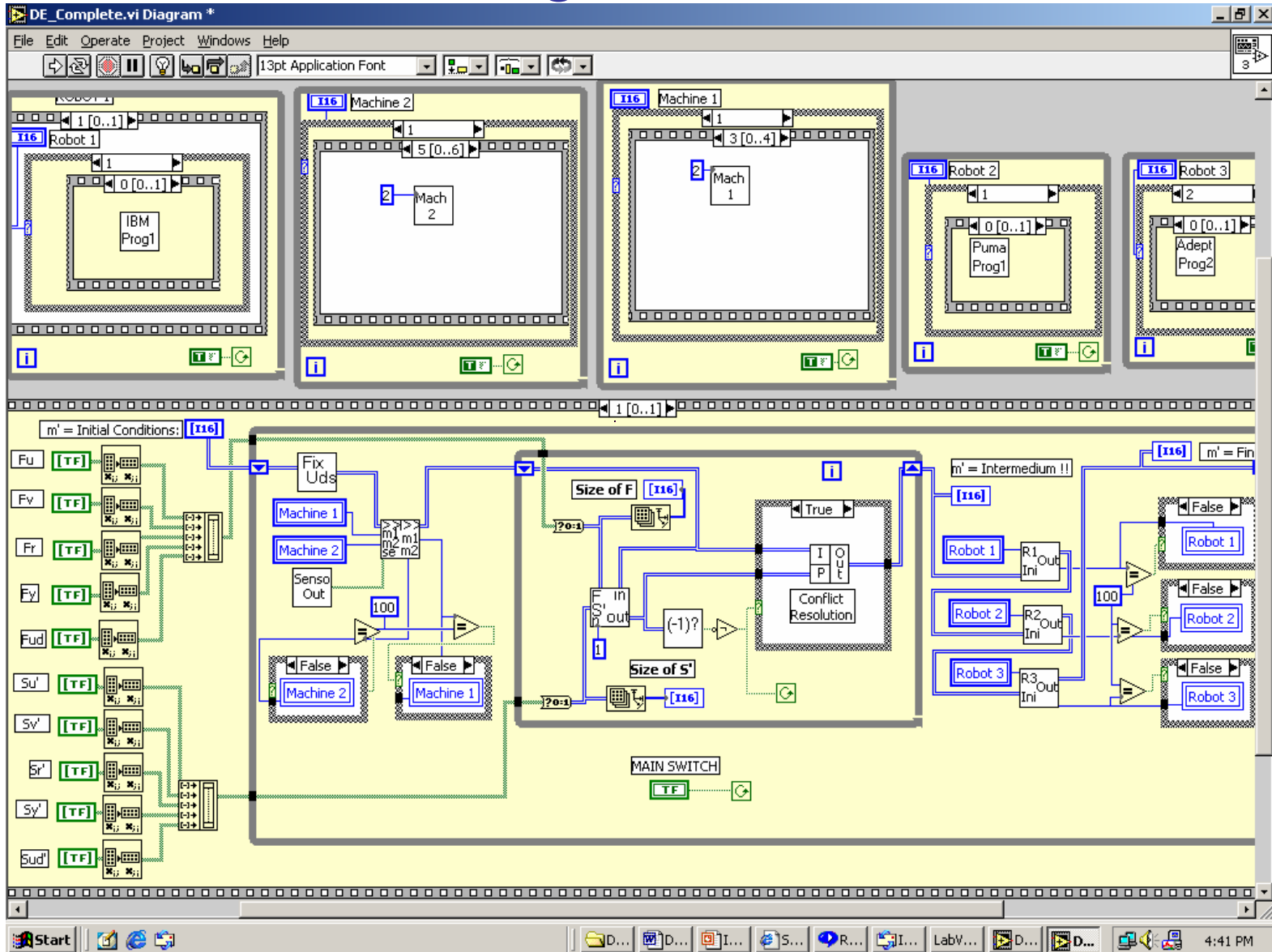
Petri Net flow chart



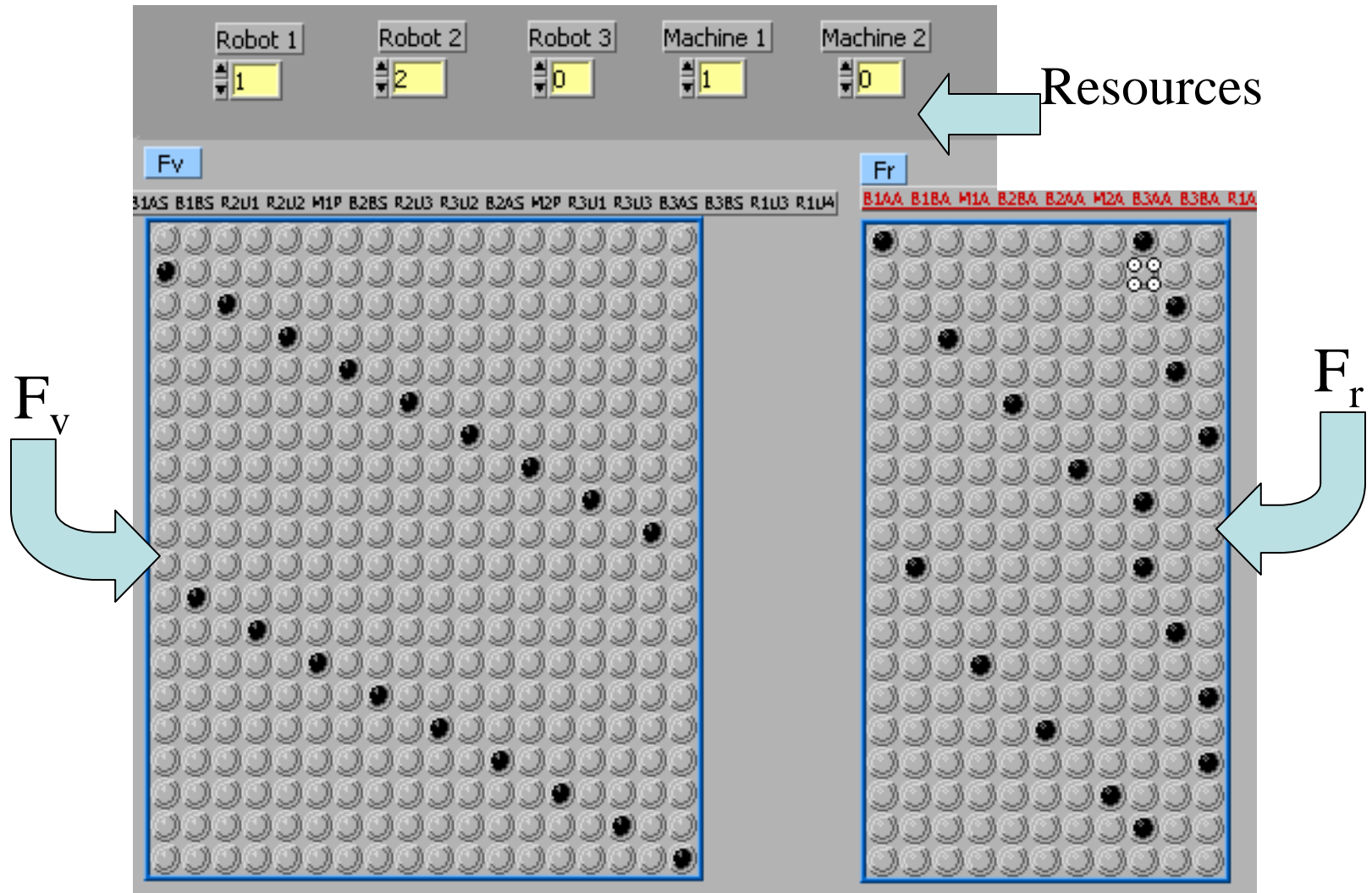
c.f. Saridis
Jim Albus



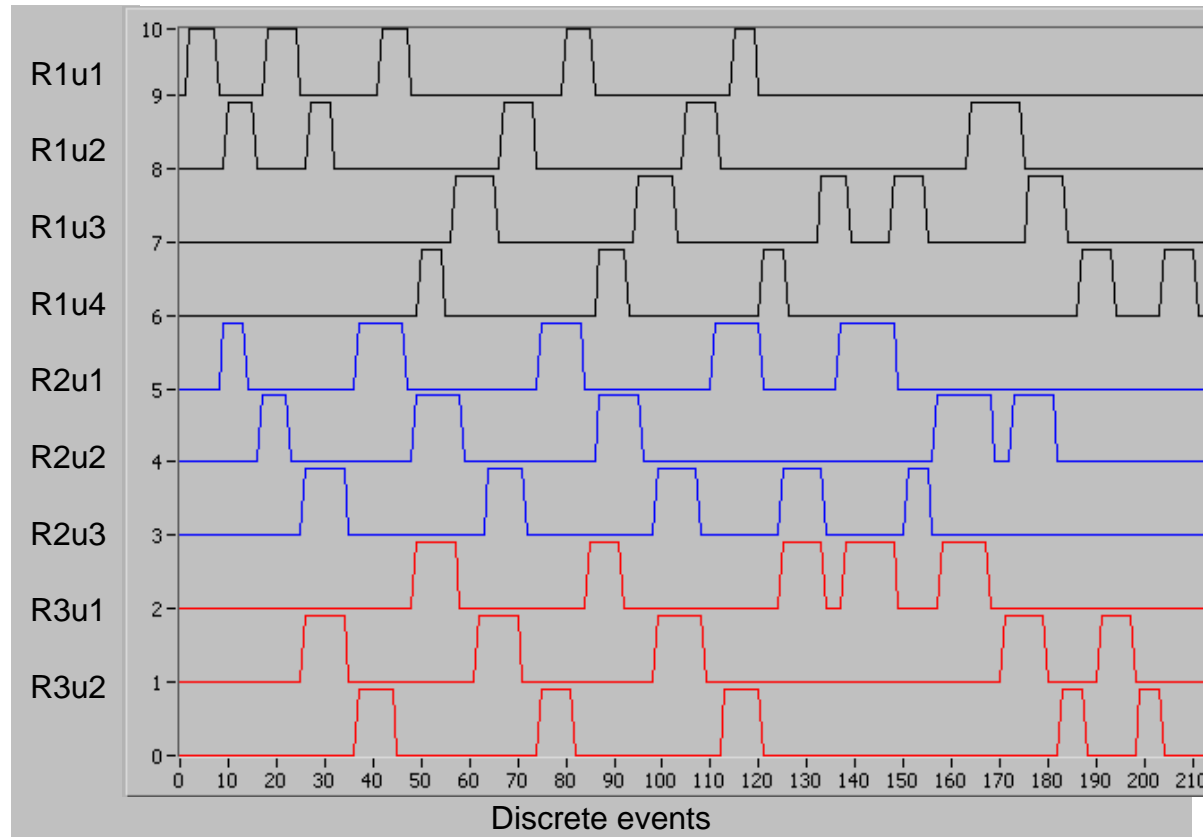
LabVIEW diagram of Controller



LabVIEW Controller's interface:



Results of LabVIEW Implementation on Actual Workcell

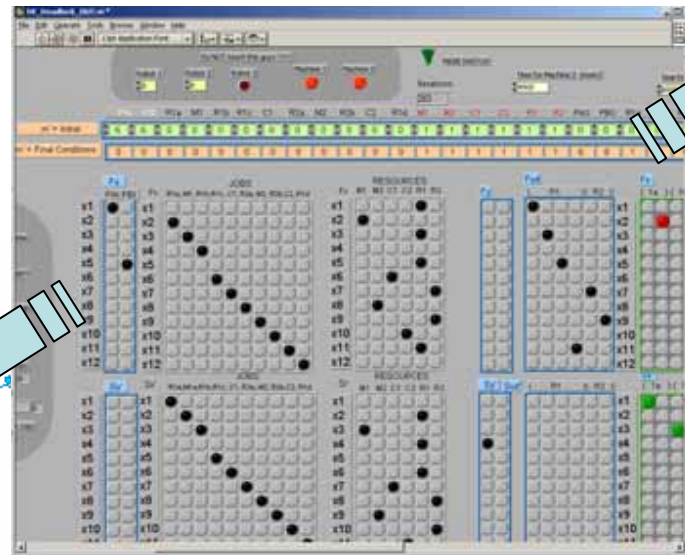
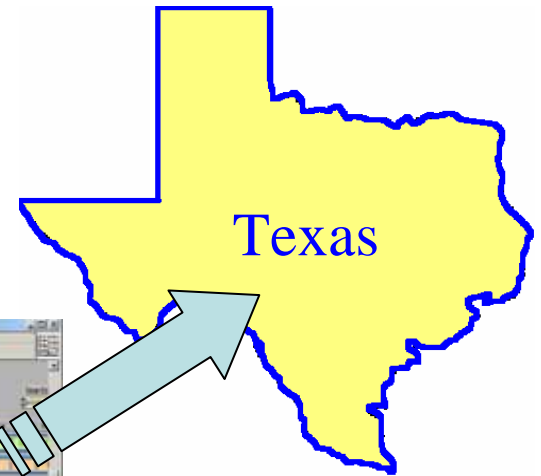


Compare with MATLAB simulation!

We can now simulate a DE controller and then implement it,
Exactly as for continuous state controllers!!

U.S.-Mexico shared research

DE control via internet



Using Matrix DEC in
LabVIEW